

# PHOTOVOLTAIC CELL MODELLING AND SIMULATION STRATEGIES

Pervez Hameed Shaikh\*, Anwar Ali Sahito\*, and Aslam Pervaiz Memon\*\*

## ABSTRACT

The main focus of this paper is on the modeling of photovoltaic panels or modules that are composed of numerous basic cells. The constituent which impact on the precision of PV simulation is the equivalent circuit modeling primarily encompasses the estimation of the non-linear I-V and P-V characteristics. The assessment, analysis and depiction of PV model will ultimately describe the parameters for the development of maximum power point tracking (MPPT) algorithm along with power conditioners compatibility. This paper intends to collectively organize and assess the mathematical model of the PV cells and to drive the best possible modeling for the continuous varying solar radiation and even under partial shade conditions.

*Keywords-Photovoltaic, non-linear, model, solar, simulation*

### Nomenclature defined in equations as follows:

- e : Charge of electron ( $1.602 \times 10^{-19}$  C).  
k : Boltzmann's constant ( $1.38 \times 10^{-23}$  J/K).  
 $I_0$  : Reverse saturation current for diode.  
 $I_{ph}$ : Photo-current, a function of junction temperature and irradiation level (5 A).  
 $I_c$  : Output current of cell, A.  
 $R_s$  : Series resistance of cell.  
 $T_c$  : Operating temp. of reference cell (20 °C).  
 $V_c$  : Output voltage of cell, V.  
 $I_{pv,n}$ : Light-generated current in Amperes at the nominal condition (usually 25 °C and 1000W/m<sup>2</sup>),  
 $\Delta T = T - T_n$  (being T and  $T_n$  the actual and nominal temperatures in Kelvin)  
 $G$  : Irradiation on the device surface in [W/m<sup>2</sup>],  
 $G_n$  : Nominal irradiation in [W/m<sup>2</sup>].  
 $E_g$  : Energy band-gap of the semiconductor at normal ambient temperatures.  
 $I_{0,n}$  : Nominal saturation current  
 $N_s$  : Cells connected in Series.  
 $N_p$  : Cells connected in Parallel.  
 $V_{t,n}$  : Thermal voltage of  $N_s$  (series-connected cells) at the nominal temperature  $T_n$ .

## 1. INTRODUCTION

Solar photovoltaic is a single stage non-conventional energy transformation source which makes electrical energy from light energy. Edmund Becquerel explained in

1839, as the action of falling of light quantum on silver glazed platinum electrode. PV cell is assemble by thin wafers of p-type and n-type material to form a junction. In dark, it has output characteristics similar to a simple diode [1]. The major benefits that PV generators possess, which has resulted in its huge utilization since last two decades, are small lead duration for designing and fixing new systems, matching of output power with peak load burdens, immobile structure, environmental friendly, portable, light weight, high efficiency per unit of weight, noise free, high useful operating life and no moving parts [2].

When PV cell is exposed to light (e.g. sunlight), photons with superior energy band gap of the semiconductor are enthralled thus creating an electron-hole pair. The inner electric fields of pn-junction will cause to be swept across and will produce current proportional to the incident irradiation.

The current flows in the external circuit when PV cell is shorted and shunted internally through intrinsic p-n junction when open circuited. Thus, setup the open circuit voltage exponential characteristics of the cell analogous to that of a diode [3]. PV cells are replicated as a bi-terminal device, which conducts as of a diode in dark and also produce electrical energy when exposed to sunlight.

The constituent which impact on the precision of PV simulation is the equivalent circuit modeling primarily

\* Assistant Professor, Department of Electrical Engineering, Mehran University of Engineering and Technology, Jamshoro, Pakistan

\*\* Professor, Department of Electrical Engineering, Quaid-e-Awam University of Engineering, Sciences and Technology, Nawabshah, Pakistan

encompasses the estimation of the non-linear I-V and P-V characteristics. The assessment, analysis and depiction of PV model will ultimately describe the algorithm parameters for the development of maximum power point tracking (MPPT) algorithm along with power conditioners [4-5].

## 2. PHOTOVOLTAIC PARAMATRIC EQUIVALENCE

Fig. 1 shows the modest form of equivalent circuit of a solar cell comprises of current source and one or two shunt diodes [5-9]. Current voltage (I-V) characterisitcs of cell are determined by the diode [1]. The output of current source is directly proportional to the incident light falling on the cell.

The equivalent circuit models are an appropriate and common approach to pronounce the electrical activities of system devices. In general, an equivalent circuit deals three core benefits:

- Easy to implement with complex electrical systems;
- Permits the system properties depiction in a homogenous and curtailed way in a simple analytical model
- Deliver insights into the multifarious physical progressions which occur within the device/system.

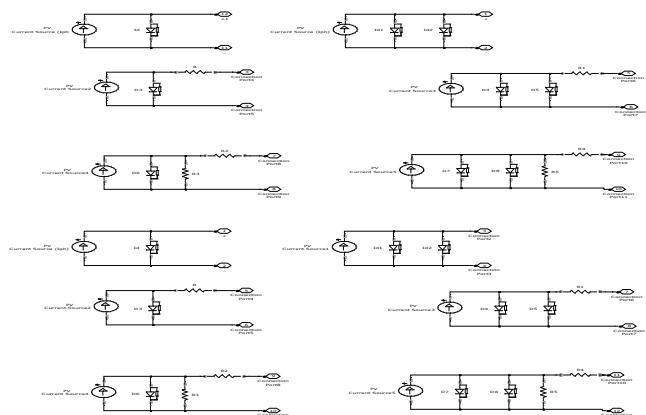


Fig. 1: Ideal Equivalent Circuit Models

### a. Ideal Photovoltaic Cell

Electrically, the photovoltaic cell is analogous to a current source in parallel with a non-linear, asymmetric resistive component, i.e., a diode (Fig. 1). Once the cell is brightened, the ideal cell generates photocurrent proportionate to the light concentration. The photocurrent is in quotient amongst the adjustable resistance of non-linear diode and the connected burden, in a ratio which hang on the resistance of connected load and radiance level. It only necessitates three parameters, explicitly; the open circuit voltage ( $V_{oc}$ ), the short-circuit current ( $I_{sc}$ ) and the diode ideality factor ( $A$ ) [10].

### b. Realist Photovoltaic Cell Parameters

In a real photovoltaic cell the power extracted from the PV cell depends on several factors which were neglected in the ideal state as defined under:

#### (i) Parasitic Resistances

In genuine PV cells, the power is dissipated in the resistance of the connections, finite conductivity of neutral regions and also the leakage currents within the sides. These possessions depict electrical equivalence to two parasitic resistances in series  $R_S$  (causes the opposition to flow of electrons and holes), its value is so small to withdraw from the circuit [5, 15, 17-19]. Shunt resistance  $R_{sh}$  (depicts recombination of electron hole pairs inside the pn junction). Shunt resistance is usually very high and is being neglected for simplification [11-13, 14-18].

#### (ii) Diode Ideality Factors

The electron hole pair alignment at the junction express the ideality factor of diode meant with 'A'. Its value is generally presumed to be 1 by several authors, referring to P-N junction formation and diffusion of charge carriers across the barrier [20]. In case of two diodes, the second diode is set equal to 2, in accord with the traps notion of recombination [21]. The ideality factor is typically constant at minute currents and ample variation is observed at high currents. This may also vary with temperature [19, 22].

#### (iii) Thermal Voltage

The diode thermal voltage due to the units of voltage, represented as

$$V_T = k_B \frac{T}{q_e} \quad (1)$$

where junction temperature ( $T$ ) is assumed to be controlled prior known extent,  $k_B$  is Boltzmann's constant, and  $q_e$  is the elementary electronic charge. Its value is typically around 26 mV at ambient temperature [23].

## 3. SINGLE DIODE MODEL

Alternatively termed one-diode or single exponential model is the modest and utmost used model for representation of PV cells. Nevertheless unpractical, the simplest PV cell equivalence is single diode model, a current source in parallel to a diode [4, 9, 15, 18, and 19]. This model is enhanced with the insertion of one series resistance,  $R_S$  [1, 12, 23-26]. In spite of its simplicity to practical approach, the proposed model unveils severe scarcities, with leakage currents within PV cells due to

impurities near the junction and inhomogeneous crystal lattice and also when endangered to temperature deviations. The value of  $R_S$  is quite small and this parameter is often ignored [22, 26 and 28].

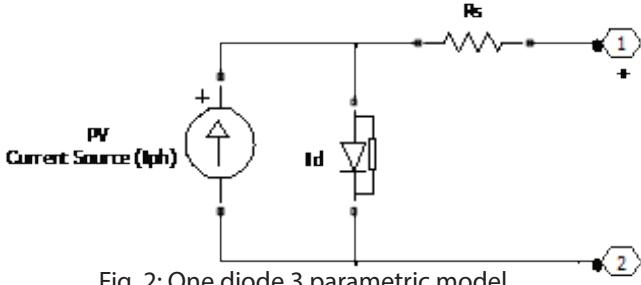


Fig. 2: One diode 3 parametric model

$$I_{pv} = I_{ph} - I_d \left( \exp \left( q \frac{V_{pv} + IR_s}{Akt} \right) \right) \quad (2)$$

A supplementary shunt resistance  $R_p$  included in it for leakage currents, non-uniform crystal fabrication structure causes model extension which burdens substantial computational effort, though improvement is achieved in its output power characteristics [20, 21, 29-31]. The value of  $R_p$  is generally neglected in [17-19] to simplify the model.

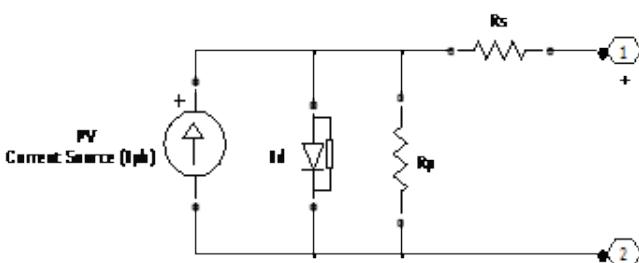


Fig. 3: One diode 4 parametric model

$$I_{pv} = I_{ph} - I_d \left( \exp \left( q \frac{V_{pv} + IR_s}{Akt} \right) \right) \frac{V_{pv} + IR_s}{R_p} \quad (3)$$

This KVL model devises the graphical current-voltage and power-voltage characteristics as shown in Fig. 4, where the three notable points are highlighted i-e open circuited voltage ( $V_{OC}$ , 0), short circuited current (0,  $I_{SC}$ ) and the maximum power point ( $V_{mp}$ ,  $I_{mp}$ ). These models are supposed to immune from recombination loss in the depletion region but at low voltage level, the recombination implies a significant power loss in PV cells. This does not satisfactorily express in the single exponential model. Thus an addition of another shunt diode will comprehensively show this recombination loss.

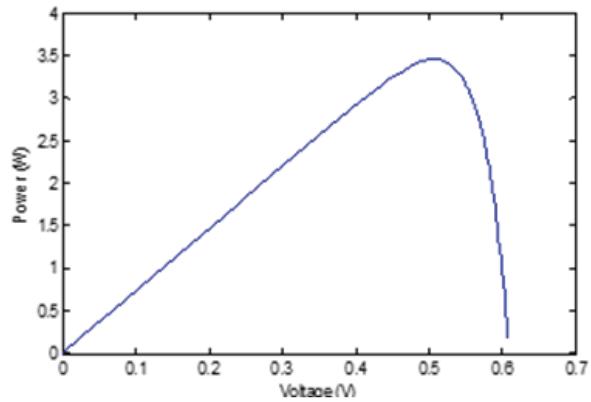
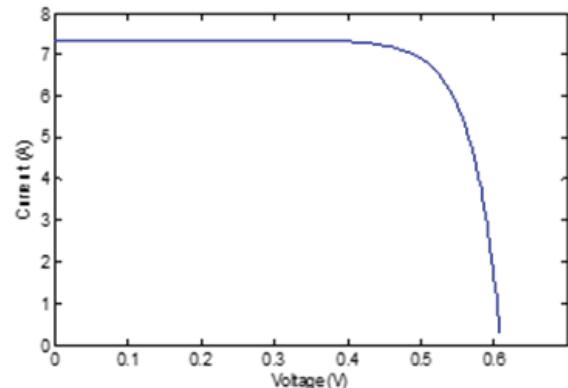


Fig. 4: PV cell characteristics; I-V and P-V (MATLAB ®)

#### 4. TWO-DIODE-MODEL FOR PV CELLS

An even more exact modeling could be achieved by the double-diode or double exponential model with like or unlike diode ideality factors, are joined in parallel. This recombination loss concern in depletion region at low voltage level leads to a more precise model with the addition of another shunt diode for the depiction of the substantial loss [31]. Consideration of this loss leads to a more precise model known as the two-diode model [32]. This model has the benefit of improved precision but has the hindrance of dependency on increased number of parameters. The major impact of the proposed model is temperature variation sensitivity increases as the saturation current is doubled.

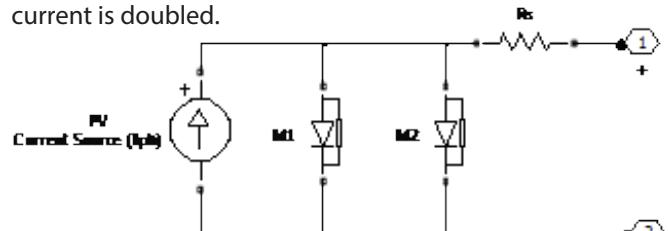


Fig. 5: Double diode 4 parametric model

$$I_{pv} = I_{ph} - I_{d1} \left( \exp \left( q \frac{V_{pv} + IR_s}{Akt} \right) \right) - I_{d2} \left( \exp \left( q \frac{V_{pv} + IR_s}{Akt} \right) \right) \quad (4)$$

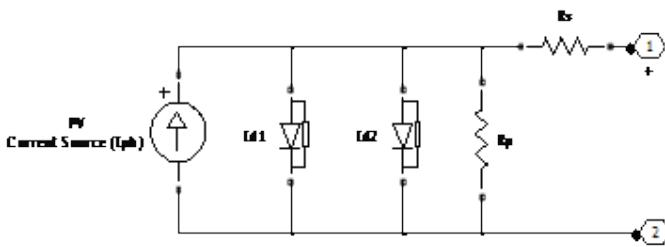


Fig. 6: Double diode 5 parametric model

$$I_{pv} = I_{ph} - I_{d1} \left( \exp \left( q \frac{V_{pv} + IR_s}{A k T} \right) \right) - I_{d2} \left( \exp \left( q \frac{V_{pv} + IR_s}{A k T} \right) \right) - \left( \frac{V_{pv} + IR_s}{R_p} \right) \quad (5)$$

- Introducing following points to the model will enhance accuracy, complexity and sophistication [4]:
- Temperature dependence of the diode saturation current  $I_0$  and the photocurrent  $I_L$ .
- A better and accurate shape between the open-circuited voltage and peak power point by a series resistance  $R_s$  which represents the internal current flow loss.
- Shunt resistance ( $R_{sh}$ ), in parallel with the diode relates to the leakage current to ground probably possess high value or being usually neglected
- Bringing two diodes in parallel with an independent set of saturation currents or letting the Q-F (quality factor) of the diode to have variable parameter insteading of making it fixed at 1 or 2.
- A fair and a common assumption for an ideal cell is  $R_s = R_{sh} = 0$ , [6]. A modest complexity model is used to reach at realistic approach.

The rational simulation time management along with the values of approximation of all of the model parameters is the core challenge. Numerous computational techniques have been already offered [17]-[20] and in all these, additional fresh coefficients are presented, ultimately causes computational effort to increase. In determining initial values of parameters, some empirical solutions are pursued. Whereas, scrutinizing its physical features such as the electron coefficient diffusion, lifespan of marginal carriers, intrinsic carrier concentration and other semiconductor parameters [21]-[24] describing the physical conduct of a cell. Since the data about semiconductor is not always accessible in PV datasheets commercially.

Different simulation software are available in market for analyzing mathematical models of the PV cell, Some of the commonly used software are PVsyst, PVcad, SolarPro, PV-DesignPro and PV-Spice. These software packages are

costly and rarely have provision of power converters to be interfaced with PV arrays [25].

## 5. DIODE MODEL JUSTIFICATION

Numerous model variants are established in collected works Watson (1960) [1, 4] offered a two-diode model with identical exponents for crystalline-Si PV cell. Wolf and Rauschenbach (1963) [4] focused the effects of dispersed series resistance PV cells, and resulting the analogous mathematical model [4], but they overlooked the loss caused by shunt current due to the high shunt resistance ( $R_P=13.8 \text{ k}\Omega$ ) consideration in their tentative 2-cm<sup>2</sup> mono-crystalline Si cell. Müllejans et al. (2004) [5] used 5-parameter model, supposing prior diode ideality factors  $n_1=1$  and  $n_2=2$ . They stated shunt resistance  $R_P$  values of practical (large-area) poly-Si cells is as low as  $6.6 \Omega$ . In [6, 8, and 13] have also implemented the similar 5-parameter version with the consideration of recombination diode insignificant. Coors and Böhm (1997) [7] have initiated IEC-891 superior 7-parameter variant and Blaesser's technique in I-V curves improvement [7].

Ouennoughi and Chegaar (1999) [13] single-diode estimate have been used and applied the classical equation to a PV module, providing option for number of series cells portraying their ideality factor. This approach thus creates the assessment of p-n junction parameters for cells and modules less straight-forward. Lo Brano et al. (2010) [14] ideality factor of diode using dimensions Volts/Kelvin integrating the fundamental charge and Boltzmann's constant. Thus, stripping  $q_e$  and  $k_B$ , classical (dimensionless) ideality factors of 0.87 and 0.73 achieved, which are not physical. The 3D effects in PV cell are investigated at [4] and also evaluating current flow configuration in distributed series resistance thus becomes too modest and precise model the output from a PV cell. Since, at-least an extra diode and an additional resistor be added for understanding localized loss mechanisms, includes partial resistance enriched recombination [15], for the PV modules tested here, we assume that none of their cells requires such complicated modeling when illuminated outdoors.

## 6. PARAMETER EXTRACTION APPROACH

### (i) Non-linear Fitting

The shunt resistance of a PV cell can be found near short circuit with linear fitting. Since this method each time may not for modules, as bypass diodes get activated at decreased voltage levels. The approximate equivalence of photo-current and short circuit current is assumed for only crystalline cells and the saturation currents in that are smaller in magnitude of several order and also the series resistance is much smaller than the shunt one. Non-linear fitting is preferred for estimation of parameters [39, 43-48]

most of them assume the fixed values of ideality diode factor 1 and 2, while selecting other parameters with fixtures. This technique requires the initial values for non-linear fitting approaches resulting satisfactory curve fits. The non-linear curve fittings are complicated in modeling and even in computer coding. Care must be taken for representative values, with less complexity observations. [47, 50 and 51]

### **(ii) Semi-log Partial Linear Fitting**

To analyze data of p-n junction [45, 52-54] and to discriminate linear part of semi-logarithmic plot, this dominates the two exponential terms. The linear region slope is  $q_e/nkV$  ( $q_e/NSnKV$  for modules) is used to extract diode ideality and current intercept for linear fit provides reverse saturation current. In [45, 53] diode ideality is temperature dependent and series resistance compensation effects the linear deviations at increased voltages. Since physically consistent parameters may not be extracted from tangents to semi logarithmic curve, as there might be conduction and recombination prevailing [55]. The series-resistance effect ( $R_s$  is normally not known prior) hence, compensated and the unfavorable effects acquire place at modest voltages, thus interfering with  $R_s$ . These all detrimental mechanisms (shunting, recombination or resistive losses) lead to slight rise in the local ideality factor at enhanced voltage level.

### **(iii) Multiple Quad Dark Analyses**

The above two methodologies reviewed may also be pertinent to dark characteristics of PV cells, used in arrangement with irradiated cells to explore certain parameters. An intrinsic difficulty of this technique is imprecise result for  $R_s$  caused by altered current drift patterns (e.g. current crowding) in brightened versus dark cells [56, 43]. Reverse current vs. voltage features are also used to find individual parameters. Dark and multiple-quadrant methods are out of scope yet; we have focused on illuminated forward bias and partial shade data.

## **7. CONCLUSION**

The exploration of PV solar cell has been augmented in last decade to confront the world energy need and improved cell/module performance features at cheaper rates. A PV cell is presumed as a large area forward bias diode p-n junction with a photo voltage, thus created from electron disorder with incident photons at junction. Most of the factors which affect the output of PV cell must be taken into consideration along with the quality issues as ripple generation and the dynamic modeling of PV cell. Since, not only the output of solar cell is reduced but also the I-V

characteristics of PV array or module are affected by the constant partial shading. The problem is further aggravated by the reverse-biasing of the shaded cells, making it a diode with high resistance, that gets over-heated when the illumination difference is fairly large. Thus, there is need for the development of appropriate model that offer benign, amiable and a comprehensive photovoltaic solar system operating under continuous partial shading conditions and changing sun position for static or BIPV systems.

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